Measures of Association in Epidemiology

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Chi square
Odds Ratio
Relative Risk or Risk Ratio
Attributable Risk



## 2X2 Table (contingency table)

		Disease		
		<b>Yes</b> (+)	No (-)	Total
	<b>Yes</b> (+)	a	b	a+b
Exposure	<b>No (-)</b>	С	d	c+d
	Total	a+c	b+d	a+b+c+d



Event	Event observed		
forecast	Yes	No	Marginal total
Yes	a	b	a+b
No	c	d	c + d
Marginal total	a+c	b+d	a + b + c + d =n

- A= Exposed, and diseased
- B= Exposed, Not diseased
- C= Not exposed, diseased
- D= Not exposed, Not diseased
- A+B+C+D=Total

Cells

5

Event	Event observed		
forecast	Yes	No	Marginal total
Yes	a	b	a + b
No	c	d	c + d
Marginal total	a+c	b+d	a + b + c + d =n

**Marginal totals** a+b= Exposed c+d= Non-exposed a+c= Diseased b+d= Non-diseased **Grand total** n = a+b+c+d

**Totals** 

#### **1. Chi-square in Cross-sectional studies**

Chi-square tests whether there is an association between two categorical variables.

For a 2X2, table:  $X^2 = n (ad - bc) - n /2)^2$ (a+b)(a+c)(c+d)(b+d)

If the calculated chi-square value is greater than the critical value or P<0.05, we say that there is a significant association between the risk factor and the disease (usually calculated using software like SPSS or excel).

Chi-square statistic tells only whether there is association. It doesn't tell us how strong an association is.

#### 2. Relative risk (RR) or Risk Ratio (RR) In a cohort study

RR: The estimation of disease risk associated with exposure (strength of association)

RR Expresses risk of developing a disease in exposed group (a + b) as compared to non-exposed group (c + d)

RR= Incidence (risk) among exposed Incidence (risk) among non-exposed

 $RR = \frac{a/(a+b)}{c/(c+d)}$ 

Event	Event observed		
forecast	Yes	No	Marginal total
Yes	a	b	a + b
No	c	d	c + d
Marginal total	a+c	b+d	a + b + c + d =n

## **Analysis in Cohort studies**

In a Cohort Study, we can calculate Incidence. So, Relative Risk can be obtained from a cohort study.

Cigarette smoking (Exposure)	Disease (with Ca lung )	No Disease (without Ca lung )	Total
Yes	70 (a)	6930 (b)	7000 (a+b)
Νο	3(c)	2997(d)	3000 (c+d)



## **RR in a Cohort Study**

#### **Incidence rates :**

Risk among exposed (smokers) = 70/7000 = 10 / 1000.

Risk among non-exposed(non smokers) = 3/3000 = 1/1000.

#### RR = <u>Risk (Incidence) among exposed</u> Risk (Incidence) among non exposed. RR = 10/1=10

The exposed have 10 times the risk of developing the disease when compared to non-exposed



## Interpretation of relative risk

What does a RR of 2 mean? Risk in exposed=2X Risk in non-exposed

Thus a relative risk of 2 means the exposed group is two times at a higher risk of developing the disease when compared to non-exposed



#### **Strength of association**

In general strength of association can be considered as: High association if RR>3 Moderate if RR is between 1.5 & 2.9 Weak association if RR is between 1.2 & 1.4 No association exists if RR is 1 **Negative association (protective effect) if RR <1** 



## 3. ODDS RATIO (OR)

Odds Ratio (OR) is a measure of the strength of the association between risk factor & outcome.

- ✓The odds ratio is the cross product of the entries in table.
- OR can be calculated in case-control studies instead of RR
- □ OR can be a good estimate of RR



## Odds ratio (OR)

Odds Ratio can be a good estimate of RR. Odds ratio is the ratio of odds of exposure among diseased to odds of exposure among nondiseased

OR = <u>Odds of exposure among diseased</u> Odds of exposure among non-diseased

= (a/c)/(b/d) = ad/bc

Interpretation of OR is the same as that of RR





#### RR can be best estimated by OR if the following conditions are fulfilled:

- 1. Controls are representative of general population
- 2. Selected cases are representative of all cases
- 3. The disease is rare



# ANALYSIS in case-control studies

Estimation of disease risk associated with exposure (odds ratio)



## **OR in a case-control study**

	Cases (with Ca lung )	Controls (without Ca lung)
Smokers	33 (a)	55 (b)
Non smokers	2 (c)	27 (d)
Total	35 (a+c)	82 (b+d)

## **OR in Case-control studies**

## Odds ratio is a key parameter in the analysis of Case-control studies

Disease

	Cases (Lung Ca)	Controls (No Lung Ca)
Smokers	a (33)	b (55)
Not smokers	c (2)	d (27)

#### Attributable Risk (AR)

AR indicates how much of the risk is due to (attributable to) the exposure.

Quantifies the excess risk in the exposed that can be attributable to the exposure, by removing the risk of the disease that occurred due to other causes.

AR= Risk (incidence) in exposed- Risk (incidence) in non-exposed

AR= [a/(a+b)] - [c/(c+d)]Attributable risk is also called risk difference.

forecast Yes	No	Manager
2019-04-04		warginal total
Yes a	b	a + b
No c	d	c + d
Marginal total a + c	b+d	a+b+c+d=n

#### **Attributable risk percent (AR%)**

Estimates the proportion of disease among the exposed that is attributable to the exposure.

AR%= (<u>Risk in exposed – Risk in non-exposed</u>)X100% Risk in exposed

AR% = 10 - 1 X 100% = 90% (as in the previous Cohort study example) 10

90% of the lung cancer among smokers was due to their smoking.

□ This suggests the amount of disease that might be eliminated if smoking could be controlled or eliminated.

## Possible outcomes in studying the relationship between exposure & disease

1. No association **RR=1 AR=0** 2. Positive association **RR>1 AR>0** 3. Negative association **RR<1 (fraction) AR<0 (Negative)** 



#### **Risk Vs Preventive factors**

A *risk factor* is any factor positively associated with a disease (RR>1). It is associated with an increased occurrence of a disease

- A *preventive factor* is any factor negatively associated with a disease (RR<1). It is associated with a decreased occurrence of a disease.
- Risk and preventive factors *may (not)* be amenable to change (e.g. Smoking, age)

## **Population Screening**

Screening is "application of a test to asymptomatic people to detect occult disease or a precursor state" (Alan Morrison, *Screening in Chronic Disease*, 1985)

- Immediate objective of a screening test to classify people as being likely or unlikely of having the disease.
- Ultimate objective: to reduce mortality and morbidity
- Many countries have national screening programs for various diseases.



## **Population Screening**



Familiar examples of the use of population screening are **cancer** screening (e.g., Pap smears to detect cervical neoplasia, mammography and physical breast exam to detect breast cancer, PSA to detect early prostate cancer, and fecal occult blood testing to detect colorectal cancer or adenomas).

Screening programs for hypertension and diabetes to prevent complications

Screening of **newborns** for phenylketonuria (PKU) to prevent mental retardation.

PCR test for Covid-19, using thermometer to detect fever).

## **Screening test**

A screening test must be accurate. There are two major dimensions to accuracy:

1. Reliability (consistent): get <u>same</u> result if we repeat it (However, a test can be reliable but still give an incorrect result).

2. Validity: give the <u>correct</u> result (reflect the true state).

There are two desirable properties for a screening test related to validity:

Sensitive: The ability to correctly classify cases as positive.

Specificity: The ability classify non-cases as negative.

Note that sensitivity and specificity are both probabilities of <u>correct</u> classification.

## Reliability

Reliability does not ensure validity, but lack of reliability constrains and jeopardizes validity.

A test that is unreliable cannot be valid. The opposite is not true, however (a reliable test may or may not be valid).

Even if test-retest agreement is very high (for example, 100%), the test could simply be consistently incorrect.

e.g. measurement of blood pressure using sphygmomanometer, temperature using thermometer.



## Validity

**1. Sensitivity of the test:** the probability of correctly classifying someone who has the disease (case).

Probability (proportion) of <u>correct classification of cases</u> :

#### Cases found by the test as + / all cases

2. Specificity of the test: the probability of correctly classifying someone without the disease (healthy, non-case).
 Probability (proportion) of correct classification of non-cases:

Non-cases found by the test as - all non-cases







## Sensitivity and Specificity

Number of true positives

 $Sensitivity = \frac{1}{(Number of true positives + Number of false negatives)}$ 

Number of true positives

Total number of individuals with the illness

Number of true negatives

 $Specificity = \frac{1}{(Number of true negatives + number of false positives)}$ 

Number of true negatives

Total number of individuals without the illness

#### True Disease Status





#### True Disease Status





## Interpreting test results: predictive value

Probability (proportion) <u>of those tested</u> who are <u>correctly</u> <u>classified by the test:</u>

**Positive predictive value** = Cases identified / all positive tests **Negative predictive value** = Non-cases identified / all negative tests



#### True Disease Status





#### True Disease Status



